

# Prospects for detecting exoplanets around double white dwarfs with LISA and Taiji

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## 1. Abstract

★ Recently, [Tamanini & Danielski \(2019\)](#) discussed the possibility to detect circumbinary exoplanets (CBPs) orbiting double white dwarfs (DWDs) with the Laser Interferometer Space Antenna (LISA). Extending their methods and criteria, we discuss the prospects for detecting exoplanets around DWDs **not only by LISA, but also by Taiji**, a Chinese space-borne gravitational-wave (GW) mission that has slightly better sensitivity at low frequencies.

★ We first explore how **different binary masses and mass ratios** affect the abilities of LISA and Taiji to detect CBPs. Second, for certain **known detached DWDs** with high signal-to-noise ratios, we quantify the possibility of CBP detections around them. Third, based on the DWD population obtained from the Mock LISA Data Challenge, we present basic assessments of the **CBP detections in our Galaxy** during a 4 year mission time for LISA and Taiji.

★ We discuss the **constraints on the detectable zone** of each system, as well as the distributions of the inner/outer edge of the detectable zone. Given the DWD population, we further inject two different planet distributions with an occurrence rate of 50% and **constrain the total detection rates**. We briefly discuss the prospects for **detecting habitable CBPs around DWDs** with a simplified model. These results can provide helpful inputs for upcoming exoplanetary projects and help analyze planetary systems after the common envelope phase.

## 2. Method

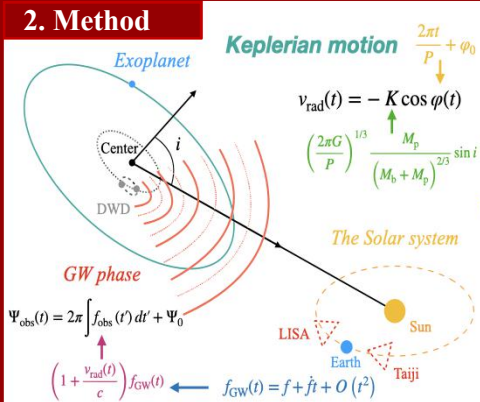


Figure 1. Illustration of changes on the observed GW frequency through the Doppler effect

$$h_{\text{fit}}(t, \lambda) = \frac{\sqrt{3}}{2} A_{\text{LISA}} \cos \left[ \Psi_{\text{obs}}(t) + \Phi_{\text{LISA}}^{\text{fit}}(t) + \Phi_{\text{D}}(t) \right]$$

$$\lambda = \left\{ \ln(\lambda), \Psi_0, f, \dot{\lambda}, \theta_0, \phi_0, \phi_s, \theta_s, K, P, \varphi_0 \right\}$$

True value  $\lambda$  vs Measured value  $\hat{\lambda}$ .  $\delta \lambda \equiv \hat{\lambda} - \lambda$  is a Gaussian distribution.

$$p(\delta \lambda) = p^{(0)}(\delta \lambda) \exp \left[ -\frac{1}{2} \Gamma_{ij} \delta \lambda_i \delta \lambda_j \right]$$

Fisher matrix  $\Gamma_{ij} \equiv \left\langle \frac{\partial h}{\partial \lambda_i} \middle| \frac{\partial h}{\partial \lambda_j} \right\rangle$  Fisher analysis [Cutler & Flanagan, 1994]

Parameter's variance-covariance matrix  $\Sigma_{ij} = \langle \delta \lambda_i \delta \lambda_j \rangle = (\Gamma^{-1})_{ij}$

$$\left. \begin{array}{l} \frac{\Delta K}{K} \\ \frac{\Delta P}{P} \end{array} \right\} \text{Detection criterion}$$

## 3. Detectors

**LISA**  
ESA-led: [ Amaro-Seoane et al., 2017 ]

**VS**

**Taiji**  
China: [ Ziren Luo et al., 2020 ]

## 4. Results

For known DWDs:

< 13 M<sub>J</sub>?

Source	Taiji				LISA				
	$a_{\text{min}}$ [au]	$M_p^{\text{min}}$ [M <sub>J</sub> ]	IDZ	ODZ	SNR	$M_p^{\text{min}}$ [M <sub>J</sub> ]	IDZ	ODZ	SNR
ZTF J153932.16+502738.8	1.53	1.39	0.20	2.20	124.51	2.11	0.32	2.12	81.89
SDSS J065133.34+284423.4	1.79	2.34	0.31	2.04	117.18	2.95	0.49	2.00	92.83
SDSS J083506.92+441107.0	2.03	4.76	0.73	2.21	139.66	9.50	1.40	2.12	70.02
SDSS J232230.20+050942.06	1.59	10.47	1.35	1.66	70.72	21.27	-	-	34.82

Table 1. Possible detections of CBPs around known DWDs

For MLDC Round 4:

SNR ≥ 10

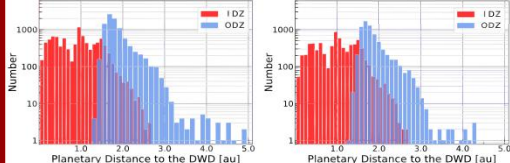
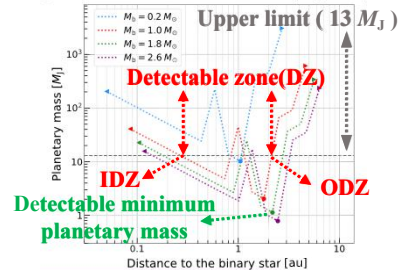


Figure 3. Distributions of IDZ and ODZ for promising systems  
Left: Taiji (9053) Right: LISA (6718)

## 5. Conclusions

- I. Complementary to electromagnetic methods;
- II. Comparisons between Taiji (better) and LISA;
- III. Possible detections (around known DWDs; in the whole Galaxy; habitable CBPs).

Figure 2. Selection functions (e.g. Taiji)



For different CBP models: OR: 50%

- Case A:  $\log U_0 (0.1 - 200 \text{ au})$ ;  $U_{M_p} (1M_{\oplus} - 0.08M_{\odot})$   
 ※ 40 (0.16%) for Taiji  
 ※ 16 (0.10%) for LISA
- Case B:  $U_0 (0.1 - 200 \text{ au})$ ;  $U_{M_p} (1M_{\oplus} - 0.08M_{\odot})$   
 ※ 2 (0.008%) for Taiji  
 ※ 0 (0%) for LISA

Note: Total detached DWDs (4-year)  
25016 (15903) for Taiji (LISA)

For habitable CBPs: Fixed luminosity

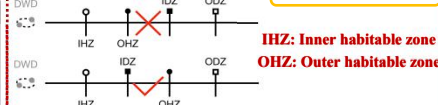


Table 2. Possible detections of CBPs around promising systems

Detector	Chicks 0%				Chicks 50%				Chicks 100%			
	IHZ	OHZ	IDZ	ODZ	IHZ	OHZ	IDZ	ODZ	IHZ	OHZ	IDZ	ODZ
Taiji	0.895	1.027	0.013	0.021	0.72	1.95	0.010	0.028	0.485	2.4	0.0020	0.034
LISA	1	0.00195	1	0.00195	1	0.00195	1	0.00195	3	0.4573	1	0.4573

## 6. References

- Danielski, C. et al., 2019, *AstronAstrophys.*, 632, A113
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- Amaro-Seoane, P., et al., 2017, arXiv:1702.00786
- Luo, Z. et al., 2020, *Results in Physics*, 16, 102918 ...